

# ESSENTIALS OF CHEMICAL REACTION ENGINEERING

SECOND EDITION

H. SCOTT FOGLER



PRENTICE HALL INTERNATIONAL SERIES IN THE  
PHYSICAL AND CHEMICAL ENGINEERING SCIENCES



*Essentials  
of Chemical  
Reaction  
Engineering*

*Second Edition*

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H. SCOTT FOGLER

Ame and Catherine Vennema Professor of Chemical Engineering  
and the Arthur F. Thurnau Professor  
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*Dedicated to*

*Janet Meadors Fogler*

*For her companionship, encouragement,  
sense of humor, love, and support throughout the years*

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# Preface

The man who has ceased to learn ought not to be allowed  
to wander around loose in these dangerous days.

—M. M. Coady

## A. Who Is the Intended Audience?

This book and interactive Web site is intended for use as both an undergraduate-level and a graduate-level text in chemical reaction engineering. The level will depend on the choice of chapters, the *Professional Reference Shelf (PRS)* material (from the companion Web site) to be covered, and the type and degree of difficulty of problems assigned. It was written with today's students in mind. It provides instantaneous access to information; does not waste time on extraneous details; cuts right to the point; uses more bullets to make information easier to access; and includes new, novel problems on chemical reaction engineering (e.g., solar energy). It gives more emphasis to chemical reactor safety (Chapters 12 and 13) and alternative energy sources—solar (Chapters 3, 8, and 10) and biofuel production (Chapter 9). The graduate material on topics such as effectiveness factors, nonideal reactors, and residence time distribution is on the Web site in PDF Chapters 14–18 (e.g., <http://www.umich.edu/~elements/5e/14chap/obj.html>).

## B. What Are the Goals of This Book?

### B.1 To Have Fun Learning Chemical Reaction Engineering (CRE)

Chemical reaction engineering (CRE) is one of two core courses that is unique to chemical engineering and that separates the chemical engineer from other engineers. CRE is a great subject that is fun to learn and is the heart of chemical engineering. I have tried to provide a little Michigan humor as we go. Take a look at the humorous YouTube videos (e.g., “Black Widow” or “Chemical Engineering Gone Wrong”) that illustrate certain principles in the text. These videos were



made by chemical engineering students at the universities of Alabama and Michigan. In addition, I have found that students very much enjoy the Interactive Computer Games (ICGs) that, along with the videos, are linked from the CRE homepage (<http://www.umich.edu/~elements/5e>).

### B.2 To Develop a Fundamental Understanding of Reaction Engineering

The second goal of this book is to help the reader clearly understand the fundamentals of CRE. This goal is achieved by presenting a structure that allows the reader to solve reaction engineering problems *through reasoning rather than through memorization and recall* of numerous equations and the restrictions and conditions under which each equation applies. The algorithms presented in the text for reactor design provide this framework, and the homework problems give the reader practice using the algorithms described in Figures P-1 and P-2, shown in Preface Section C. The conventional homework problems at the end of each chapter are designed to reinforce the principles in the chapter. These problems are about equally divided between those that can be solved with a calculator and those that require a personal computer with a numerical software package, such as Polymath, Wolfram, MATLAB, AspenTech, or COMSOL.

To give a reference point as to the level of understanding of CRE required in the profession, a number of reaction engineering problems from the California Board of Registration for Civil and Professional Engineers—Chemical Engineering Examinations (PECEE) are included in the text.<sup>1</sup> Typically, these problems should each require approximately 30 minutes to solve.

Finally, the companion Web site has been extensively revised and expanded. The updated site includes *Computer Simulations and Experiments* with Living Example Problems that facilitate Inquiry Based Learning (IBL),<sup>2</sup> discussed in Preface Section D.2. The companion Web site includes Interactive Summary Notes of the material in each chapter, PowerPoint slides of class lecture notes, expanded derivations, YouTube Videos, Web Modules, i>clicker Questions, and Self-Tests. A complete description of these learning resources is in Appendix I.

### B.3 To Enhance Thinking Skills

A third goal of this text is to enhance *critical thinking skills* and *creative thinking skills*. How does the book help enhance your critical and creative thinking skills? We discuss ways to achieve this enhancement in Sections I.1 Critical Thinking and I.2 Creative Thinking of the Preface and on the Web sites (<http://www.umich.edu/~scps/html/06chap/frames.htm>) and (<http://www.umich.edu/~scps/html/07chap/frames.htm>).

<sup>1</sup> The permission for use of these problems—which, incidentally, may be obtained from the Documents Section, California Board of Registration for Civil and Professional Engineers—Chemical Engineering, 1004 6th Street, Sacramento, CA 95814, is gratefully acknowledged. (Note: These problems have been copyrighted by the California Board of Registration and may not be reproduced without its permission.)

<sup>2</sup> Adbi, A. “The Effect of Inquiry-based Learning Methods on Students’ Academic Achievement in Science Course,” *Universal Journal of Educational Research*, 2(1), 37–41 (2014). Also see Freeman, S., S. L. Eddy, M. McDonough, M. K. Smith, N. Okoroafor, H. Jordt, and M. P. Wenderoth, “Active Learning Increases Student Performance in Science, Engineering, and Mathematics,” *Proceedings of the National Academy of Sciences*, Vol. 111 No. 23, p. 8410 (2014).



## C. What Is the Structure of CRE?

### C.1 The Concepts that Form the Foundation of CRE

The strategy behind the presentation of material is to build continually on a few basic ideas in CRE to solve a wide variety of problems. These ideas, referred to as the Pillars of Chemical Reaction Engineering (Figure P-1), are the foundation on which different applications rest. They represent not only components of chemical reaction analysis, but also the physical phenomena of diffusion and contacting that affect chemical reactor design.

Figure P-2 shows the first building blocks of CRE and the primary algorithm that allows us to solve isothermal CRE problems through logic rather than memorization. We start with the *Mole Balance Building Block* (Chapter 1) and then place the other blocks one at a time on top of the others until we reach the *Evaluate Block* (Chapter 5), by which time we can solve a multitude of isothermal CRE problems. As we study each block we need to make sure we understand everything in that block and don't cut corners by leaving anything out so we don't wind up with a cylindrical block. A tower containing cylindrical blocks would be unstable and would fall apart as we study later chapters. Look at the animation at the end of Lecture 1 notes on the CRE Web site to see the CRE tower fall if one has an unstable tower with cylindrical blocks (<http://www.umich.edu/~elements/5e/lectures/umich.html>).

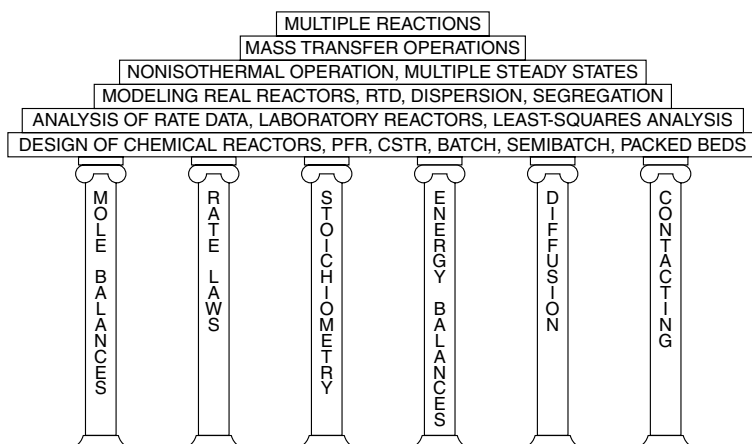


Figure P-1 Pillars of Chemical Reaction Engineering.

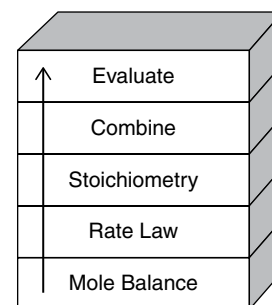
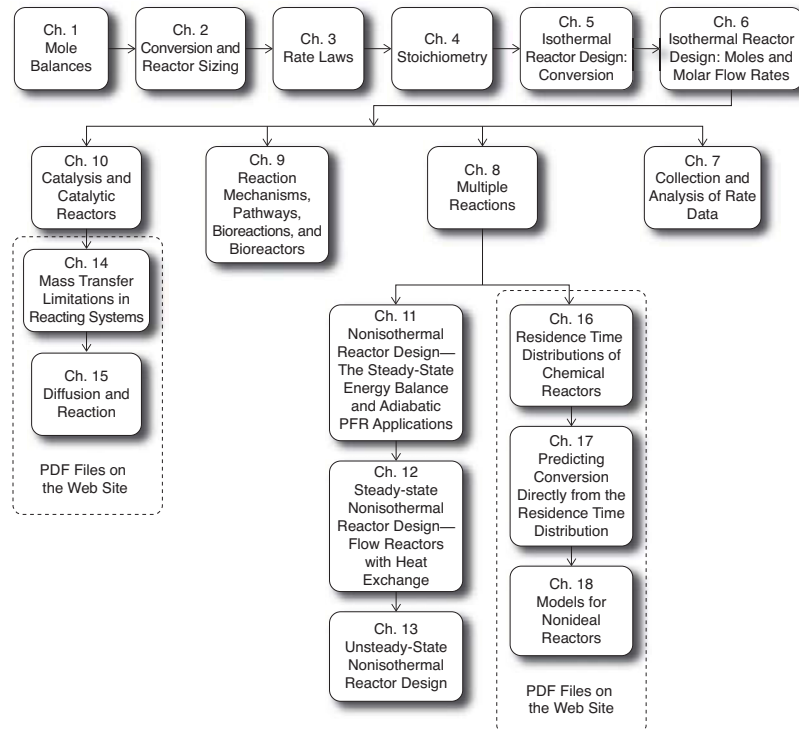


Figure P-2 Building blocks.

For nonisothermal reactions we replace the “Combine” building block in Figure P-2 with the “Energy Balance” building block because nonisothermal reactions almost always require a computer-generated solution. Consequently, we don't need the “Combine” block because the computer combines everything for us. From these pillars and building blocks, we construct our CRE algorithm:

**Mole Balance + Rate Laws + Stoichiometry + Energy Balance + Combine → Solution**

With a few restrictions, the contents of this book can be studied in virtually any order after students have mastered the first six chapters. A flow diagram showing the possible paths is shown in Figure P-3.



**Figure P-3** Sequences for study using this text.

The reader will observe that although metric units are used primarily in this text (e.g.,  $\text{kmol}/\text{m}^3$ ,  $\text{J}/\text{mol}$ ), English units are also employed (e.g.,  $\text{lb}_m/\text{ft}^3$ ,  $\text{Btu}$ ) in a few problems and examples. This choice is intentional! We believe that whereas most papers published today use the metric system, a significant amount of reaction engineering data exists in the older literature in English units. Because engineers will be faced with extracting information and reaction rate data from older literature as well as from the current literature, they should be equally at ease with both English and metric units.

## C.2 What Is the Sequence of Topics in which This Book Can Be Used?

Table P-1 shows examples of topics that can be converged in a graduate course and an undergraduate course. In a four-hour undergraduate course at the University of Michigan, approximately thirteen chapters are covered in the following order: Chapters 1 through 7 (Exam 1); Chapters 8, 11, and 12 (Exam 2); and Chapter 13 and parts of Chapters 9 and 10 (Exam 3). Chapters 14 through 18 (enclosed in dashed lines in Figure P-3) have been typeset and are available on the Web site.

### Margin Notes

There are notes in the margins, which are meant to serve two purposes. First, they act as guides or commentary as one reads through the material. Second, they identify key equations and relationships that are used to solve CRE problems.

TABLE P-1 UNDERGRADUATE/GRADUATE COVERAGE OF CRE

Undergraduate Material/Course	Graduate Material/Course
Mole Balances (Ch. 1)	Short Review (Ch. 1–8, 11–12)
Smog in Los Angeles Basin (PRS Ch. 1)	Collision Theory (PRS Ch. 3)
Reactor Staging (Ch. 2)	Transition State Theory (PRS Ch. 3)
Hippopotamus Stomach (PRS Ch. 2)	Molecular Dynamics (PRS Ch. 3)
Rate Laws (Ch. 3)	Aerosol Reactors (PRS Ch. 4)
Stoichiometry (Ch. 4)	Multiple Reactions (Ch. 8):
Reactors (Ch. 5):	Side-Fed Membrane Reactors
Batch, PFR, CSTR, PBR	Bioreactions and Reactors (Ch. 9, PRS 9.3–9.5)
Reactors (Ch. 6):	Polymerization (PRS Ch. 9)
Semibatch, Membrane	Co- and Countercurrent Heat Exchange
Data Analysis: Regression (Ch. 7)	(Ch. 12)
Multiple Reactions (Ch. 8)	Radial and Axial Gradients in a PFR
Bioreaction Engineering (Ch. 9)	COMSOL (Ch. 12)
Adiabatic Reactor (Ch. 11)	Reactor Stability and Safety (Ch. 12, 13, PRS
Steady-State Heat Effects (Ch. 12):	12.3)
PFR and CSTR with and without a	Runaway Reactions (PRS, Ch. 12)
Heat Exchanger	Catalyst Deactivation (Ch. 10)
Multiple Steady States	Residence Time Distribution (Ch. 16, 17)
Unsteady-State Heat Effects (Ch. 13)	Models of Real Reactors (Ch. 18)
Reactor Safety	Applications (PRS): Multiphase Reactors, CVD
Catalysis (Ch. 10)	Reactors, Bioreactors

## D. What Are the Components of the CRE Web Site?

The interactive companion Web site material has been significantly updated and is a novel and unique part of this book. The main purposes of the Web site are to serve as an enrichment resource and as a “professional reference shelf.” The home page for the CRE Web site (<http://www.umich.edu/~elements/5e/index.html>) is shown in Figure P-4. For discussion of how to use the Web site and text interactively, see Appendix I.

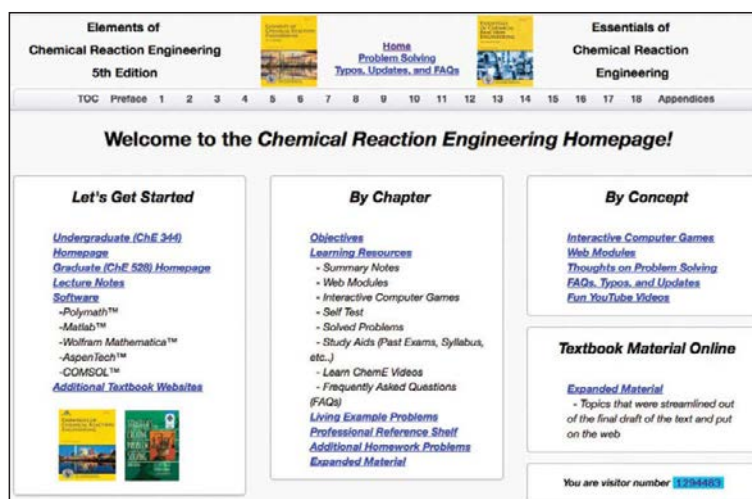


Figure P-4 Screen shot of the book's companion Web site (<http://www.umich.edu/~elements/5e/index.html>).

**The objectives of the Web site are fourfold:**

- (1) To facilitate the interactive learning of CRE by using the companion Web site and actively address the Felder/Solomon Inventory of Learning Styles discussed in Appendix I.
- (2) To provide additional technical material in the extended material and in the Professional Reference Shelf.
- (3) To provide tutorial information and self-assessment exercises such as the i>clicker questions.
- (4) To make the learning of CRE fun through the use of interactive games, LEP simulations, and computer experiments, which allow one to use Inquiry-Based Learning (IBL) to explore the concepts of CRE.

I would like to expand a bit on a couple of things that we use extensively, namely the *Chapter Resources* and the *Living Example Problems*. These items can be accessed by clicking on the chapters table of contents (TOC) bar across the top of the page. The TOC contains all the major topics. As an example, let's consider Chapter 12, for which the following screen shot shows the TOC page for Chapter 12.

The screenshot shows the Chapter 12 TOC page. At the top, there are two book covers: 'Elements of Chemical Reaction Engineering 5th Edition' and 'Essentials of Chemical Reaction Engineering Second Edition'. Below them is a TOC bar with chapters 1 through 16 and Appendices. The main content area is titled 'Chapter 12: Steady-State Nonisothermal Reactor Design: Flow Reactors with Heat Exchange'. Underneath, it lists 'Objectives' for the chapter. Below the objectives, there are 'Useful links' and 'Self test' sections.

**Figure P-5** Screen shot of Chapter 12 TOC page  
(<http://www.umich.edu/~elements/5e/12chap/obj.html>).

In addition to listing the objectives for this chapter, you will find all the major *hot buttons*, such as [Learning Resources](#), [Living Example Problems](#), and [B. i>clicker questions](#). We will now discuss each of these hot buttons in detail.

## D.1 Learning Resources

The Learning Resources give an overview of the material in each chapter through the Interactive Summary Notes. These notes include on-demand derivations of key equations, audio explanations, additional examples, and self-tests to help reinforce the principles of CRE. Additional resources include Interactive Computer Games (ICG), computer simulations and experiments, Web modules of novel applications of CRE, solved problems, study aids, Frequently Asked Questions (FAQs), Microsoft PowerPoint lecture slides, and links to LearnChemE videos. These resources are described in Appendix I.

## D.2 Living Example Problems (LEPs)



What are LEPs? LEPs are *Living Example Problems* that have solutions on the Web that allow you to change the value of a parameter and see its effect on the answer. LEPs have been unique to this book since their invention and inclusion in the third edition of *Elements of Chemical Reaction Engineering* in 2001. The LEPs use simulation software (e.g., Polymath's Ordinary Differential Equation (ODE) solvers, Wolfram, and MATLAB), which one can load directly onto their own computers to “play with” the key variables and assumptions. Using the LEPs to explore the problem and asking “What if...?” questions provide students with the opportunity to practice critical and creative thinking skills. To guide students in using these simulations, questions for each chapter (e.g., <http://www.umich.edu/~elements/5e/12chap/obj.html>) are given on the Web site. See Preface Section D.11 for ideas on how to use the LEPs.

It has been shown that students using *Inquiry Based Learning* (IBL) have a much greater understanding of information than students educated by traditional methods (*Universal Journal of Education Research*, 2(1), 37–41 (2014)).<sup>3</sup> The learning was most definitely enhanced when it came to questions that required interpretation such as, “Why did the temperature profile go through a minimum?” Each chapter has a section on *Computer Simulations and Experiments* that will guide students in practicing IBL. Students have commented that the Wolfram slider LEPs are a very efficient way to study the operation of a chemical reactor. For example, one can carry out a simulation experiment on the reactor (e.g., LEP 12-2) to investigate what conditions would lead to unsafe operation.

## D.3 Expanded Material

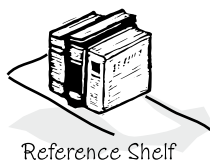
The expanded material includes derivations, examples, and novel applications of CRE principles that build on the CRE algorithm in the text.

## D.4 YouTube Videos

Here, you will find links to humorous YouTube videos made by students in Professor Alan Lane's 2008 chemical reaction engineering class at the University of Alabama, as well as videos from the University of Michigan's 2011 CRE class, which includes the ever-popular chemical engineering classic, “Reaction Engineering Gone Wrong.”

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<sup>3</sup> Ibid. Adbi, A.



### D.5 Professional Reference Shelf

This material is important to the practicing engineer, such as details of the industrial reactor design for the oxidation of  $\text{SO}_2$  and design of spherical reactors and other material that is typically not included in the majority of chemical reaction engineering courses.

### D.6 Computer Simulations Problems

These problems help guide students to understand how the parameters and operating conditions affect the reaction and the reactors. These problems are in the printed version of the second edition of *Essentials of Chemical Reaction Engineering*, but not in the printed version of the fifth edition of *Elements of Chemical Reaction Engineering*.

### D.7 Web Modules

The Web Modules are a number of examples that apply key CRE concepts to both standard and nonstandard reaction engineering problems (e.g., glow sticks, the use of wetlands to degrade toxic chemicals, and pharmacokinetics of death from a cobra bite). The Web Modules can be loaded directly from the CRE Web site ([http://www.umich.edu/~elements/5e/web\\_mod/index.html](http://www.umich.edu/~elements/5e/web_mod/index.html)).

### D.8 COMSOL

The COMSOL Multiphysics software is a partial differential equation solver that is used with Chapters 12 and 18 to view both axial and radial temperature and concentration profiles. For users of this text, COMSOL has provided a special Web site that includes a step-by-step tutorial, along with examples. See <http://www.comsol.com/ecre>. Further details are given in Appendix D.

### D.9 i>clicker Questions

i>clicker questions have been added for every chapter. Students can use these to test their understanding by viewing and responding to multiple-choice questions and then seeing the answer.

### D.10 Exercises

This section includes additional problems that can be used for studying for exams.

### D.11 Tutorials

Next, let's click on the Living Example Problems hot button shown in Figure P-5 and then click on Chapter 12 [Living Example Problems](#) to display Figure P-6.

You will note the tutorials listed just below the screen shot of the Living Example Problems page. There are 11 Polymath Tutorials, and one LEP Tutorial for each of Polymath, Wolfram, and MATLAB. There are also six COMSOL

**Chapter 12: Steady-State Nonisothermal Reactor Design: Flow Reactors with Heat Exchange**

**Living Example Problems**

The following examples can be accessed with Polymath™, MATLAB™, or Wolfram CDF Player™.

Living Example Problem	Polymath™ Code	Matlab Code	Wolfram CDF Code*	AspenTech™
LEP Table 12-2 computer experiment	LEP-12-2.pol	LEP-12-2.zip	LEP-12-2.cdf	--
Example 12-1 Isomerization of Normal Butane with Heat Exchanger	a) Co-current: LEP-12-1a.pol b) Counter-current: LEP-12-1b.pol c) Constant T <sub>a</sub> : LEP-12-1c.pol d) Adiabatic: LEP-12-1d.pol	a) Co-current: LEP-12-1a.zip b) Counter-current: LEP-12-1b.zip c) Constant T <sub>a</sub> : LEP-12-1c.zip d) Adiabatic: LEP-12-1d.zip	a) Co-current: LEP-12-1a.cdf b) Counter-current: LEP-12-1b.cdf c) Constant T <sub>a</sub> : LEP-12-1c.cdf d) Adiabatic: LEP-12-1d.cdf	--
Example 12-2 Production of Acetic Anhydride	a) Adiabatic: LEP-12-2a.pol b) Constant T <sub>a</sub> : LEP-12-2b.pol c) Co-current: LEP-12-2c.pol d) Counter-current: LEP-12-2d.pol	a) Adiabatic: LEP-12-2a.zip b) Constant T <sub>a</sub> : LEP-12-2b.zip c) Co-current: LEP-12-2c.zip d) Counter-current: LEP-12-2d.zip	a) Adiabatic: LEP-12-2a.cdf b) Constant T <sub>a</sub> : LEP-12-2b.cdf c) Co-current: LEP-12-2c.cdf d) Counter-current: LEP-12-2d.cdf	a) Adiabatic: Tutorial, ASPEN Backup File b) Constant Heat Exchange: Tutorial, ASPEN Backup File

1. **LEP** : Click [here](#) to view LEP Tutorials  
 2. **Polymath** : Click [here](#) to view Polymath Tutorials  
 3. **Matlab** : Click [here](#) to view Matlab Tutorials  
 4. **Wolfram** : Click [here](#) to download Wolfram CDF Player. You can run the CDF code, download Wolfram CDF Player for free. Click [here](#) to view Wolfram Tutorials

**Figure P-6** Screen shot of Living Examples App  
 (<http://www.umich.edu/~elements/5e/12chap/live.html>).

tutorials. To access the LEP software you want to use, i.e., Polymath, Wolfram, or MATLAB, just click on the appropriate hot button, and then load and run the LEPs in the software you have chosen. Homework problems using the LEPs have been added to each chapter that require the use of Wolfram and Polymath. The use of Wolfram will allow students to get a thorough understanding of the *Computer Simulation Problems*.

### D.12 Complete Chapters 14–18 (PDF Files)

These PDF chapters contain material that is most often included in graduate courses. However, undergraduate reaction engineering courses at a number of schools select 1–3 lectures on graduate topics, such as effectiveness factors. Therefore, the graduate course material is included on the Web site in PDF Chapters 14–18 (e.g., [http://www.umich.edu/~elements/5e/14chap/Fogler\\_Web\\_Ch14.pdf](http://www.umich.edu/~elements/5e/14chap/Fogler_Web_Ch14.pdf)).

## E. Why Do We Assign Homework Problems?

The working of homework problems facilitates a true understanding of CRE. After reading a chapter the student may feel they have an understanding of the material. However, when attempting a new or slightly different application of CRE in a homework problem, students sometimes need to go back and re-read different parts of the chapter to get the level of understanding needed to eventually solve the homework problem.

It is recommended that students first work through *Computer Simulation Problems* before going on to other problems. The end-of-chapter problems



numbered “2” (e.g., P3-2<sub>A</sub>, P12-2<sub>B</sub>) ask questions about the example problems in that chapter. These example problems are a key resource. These number-2-level problems should be worked before tackling the more challenging homework problems in a given chapter. The subscript letter (A, B, C, or D) after each problem number denotes the difficulty of the problem (i.e., A = easy; D = difficult).

## F. Are There Other Web Site Resources?

**CRE Web Site** (<http://www.umich.edu/~elements/5e/index.html>). A complete description of all the educational resources and ways to use them can be found in Appendix I.

### **What Entertainment Is on the Web Site?**

- A. YouTube Videos.** The humorous videos are discussed in section D, *What are the Components of the CRE Web Site*, above.
- B. Interactive Computer Games (ICGs).** Students have found the Interactive Computer Games to be both fun and extremely useful for reviewing the important chapter concepts and then applying them to real problems in a unique and entertaining fashion. The following ICGs are available on the Web site:

- Quiz Show I (Ch. 1)
- Reactor Staging (Ch. 2)
- Quiz Show II (Ch. 4)
- Murder Mystery (Ch. 5)
- Tic Tac (Ch. 5)
- Ecology (Ch. 7)
- The Great Race (Ch. 8)
- Enzyme Man (Ch. 9)
- Catalysis (Ch. 10)
- Heat Effects I (Ch. 12)
- Heat Effects II (Ch. 12)

As you play these interactive games, you will be asked a number of questions related to the corresponding material in the textbook. The ICG keeps track of all the correct answers and at the end of the game displays a coded performance number that reflects how well you mastered the material in the text. Instructors have a manual to decode the performance number.

## G. How Can One’s Critical Thinking and Creative Thinking Skills Be Enhanced?

(<http://umich.edu/~scps/html/probsolv/strategy/crit-n-creat.htm>)

### G.1. Enhance Critical Thinking Skills

A third goal of this book is to enhance critical thinking skills. How does one enhance their critical thinking skills? Answer: By learning how to ask the critical thinking questions in Table P-2 and carry out the actions in Table P-3. A number of homework problems have been included that are designed for this purpose. Socratic questioning is at the heart of critical thinking, and a number of homework problems draw from R. W. Paul’s six types of Socratic questions,<sup>4</sup> shown in Table P-2 and given in the expanded material on the Web site.

<sup>4</sup> R. W. Paul, *Critical Thinking* (Santa Rosa, CA: Foundation for Critical Thinking, 1992).

It is important to know these six types and be able to apply them when investigating a problem such as “Is there a chance the reactor will run away and explode?” or “Why did the reactor explode?”

Another important skill is to be able to examine and challenge someone’s hypothesis or statement. An algorithm to make this challenge is *Structured Critical Reasoning* (<http://www.umich.edu/~scps/html/O3chap/frames.htm>), developed by Professors Marco Angelini and Scott Fogler while on sabbatical at University College London (<http://www.umich.edu/~elements/5e/toc/SCPS,3rdEdBookCh03.pdf>).

Critical thinking skills are like any skill, they must be practiced. Scheffer and Rubenfeld<sup>5,6</sup> describe how to practice critical thinking skills using the activities, statements, and questions shown in Table P-3. The reader should try to practice using some or all of these actions every day, as well as asking the critical thinking questions in Table P-1 and on the Web site.

I have found that the best way to develop and practice critical thinking skills is to use Tables P-2 and P-3 to help students write a question on any assigned homework problem and then to explain why the question involves critical thinking.

More information on critical thinking can be found on the CRE Web site in the section on Problem Solving (<http://www.umich.edu/~elements/5e/probsolv/index.htm>; SCR: [http://www.umich.edu/~elements/5e/toc/SCPS,3rdEdBook\(Ch07\).pdf](http://www.umich.edu/~elements/5e/toc/SCPS,3rdEdBook(Ch07).pdf)).

TABLE P-2 SIX TYPES OF SOCRATIC QUESTIONS USED IN CRITICAL THINKING

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(1) <i>Questions for clarification:</i> Why do you say that? How does this relate to our discussion?	“Are you going to include pressure drop in your analysis when you calculate the conversion?”
(2) <i>Questions that probe assumptions:</i> What could we assume instead? How can you verify or disprove that assumption?	“Are your catalyst particles sufficiently large to neglect pressure drop?”
(3) <i>Questions that probe reasons and evidence:</i> What would be an example?	“Could the fact that you neglected pressure drop be the reason that the predicted conversion is much larger than the measured conversion?”
(4) <i>Questions about viewpoints and perspectives:</i> What would be an alternative?	“Because the pressure drop is large, would it be reasonable to increase the catalyst particle size?”
(5) <i>Questions that probe implications and consequences:</i> What generalizations can you make? What are the consequences of that assumption?	“How would your results be affected if you neglected pressure drop?”
(6) <i>Questions about the question:</i> What was the point of this question? Why do you think I asked this question?	“What led you to think about asking whether or not to include pressure drop in your calculations?”

---

<sup>5</sup> Courtesy of B. K. Scheffer and M. G. Rubenfeld, “A Consensus Statement on Critical Thinking in Nursing,” *Journal of Nursing Education*, 39, 352–359 (2000).

<sup>6</sup> Courtesy of B. K. Scheffer and M. G. Rubenfeld, “Critical Thinking: What Is It and How Do We Teach It?” *Current Issues in Nursing* (2001).

TABLE P-3 CRITICAL THINKING ACTIONS<sup>7</sup>


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<b>Analyzing:</b> separating or breaking a whole into parts to discover their nature, function, and relationships “I studied it piece by piece.” “I sorted things out.”
<b>Applying Standards:</b> judging according to established personal, professional, or social rules or criteria “I judged it according to....”
<b>Discriminating:</b> recognizing differences and similarities among things or situations and distinguishing carefully as to category or rank “I rank ordered the various....” “I grouped things together.”
<b>Information Seeking:</b> searching for evidence, facts, or knowledge by identifying relevant sources and gathering objective, subjective, historical, and current data from those sources “I knew I needed to look up/study....” “I kept searching for data.”
<b>Logical Reasoning:</b> drawing inferences or conclusions that are supported in or justified by evidence “I deduced from the information that....” “My rationale for the conclusion was....”
<b>Predicting:</b> envisioning a plan and its consequences “I envisioned the outcome would be....” “I was prepared for....”
<b>Transforming Knowledge:</b> changing or converting the condition, nature, form, or function of concepts among contexts “I improved on the basics by....” “I wondered if that would fit the situation of ....”

---

## G.2 Enhance Creative Thinking Skills

The fourth goal of this book is to help enhance creative thinking skills. This goal is achieved by using a number of problems that are open-ended to various degrees. With these, students can practice their *creative skills* by exploring the example problems, as outlined at the beginning of the home problems of each chapter, and by making up and solving an original problem. Problem P5-1 in the text gives some guidelines for developing original problems. A number of techniques that can aid students in practicing and enhancing their creativity<sup>8</sup> can be found in Fogler, LeBlanc, and Rizzo<sup>9</sup> (and its companion Web site), *Strategies for Creative Problem Solving, Third Edition* (<http://www.umich.edu/~scps/html/06chap/frames.htm>). The Web site for that book can be accessed from the CRE Web site home page. We use these techniques, such as Osborn’s checklist and de Bono’s lateral thinking (which involves considering other people’s views and responding to random stimulation) to answer add-on questions such as those in Table P-4. Mental blocks to idea generation can be found in

<sup>7</sup> R. W. Paul, *Critical Thinking* (Santa Rosa, CA: Foundation for Critical Thinking, 1992); B. K. Scheffer and M. G. Rubinfeld, “A Consensus Statement on Critical Thinking in Nursing,” *Journal of Nursing Education*, 39, 352–359 (2000).

<sup>8</sup> Creativity: <http://www.umich.edu/~scps/html/06chap/frames.htm>.

<sup>9</sup> H. S. Fogler, S. E. LeBlanc, with B. Rizzo, *Strategies for Creative Problem Solving*, 3rd ed. (Upper Saddle River, N.J.: Prentice Hall, 2014), <http://www.umich.edu/~scps/>.

TABLE P-4 PRACTICING CREATIVE THINKING

- 
- (1) Use lateral thinking to brainstorm ideas to ask another question or suggest another calculation that can be made for this homework problem.
  - (2) Use lateral thinking to brainstorm ways you could work this homework problem incorrectly.
  - (3) Use lateral thinking to brainstorm ways to make this problem easier or more difficult or more exciting.
  - (4) Brainstorm a list of things you learned from working this homework problem and what you think the point of the problem is.
  - (5) Brainstorm the reasons why your calculations overpredicted the conversion that was measured when the reactor was put on stream. Assume you made no numerical errors in your calculations.
  - (6) "What if..." questions: The "What if..." questions are particularly effective when used with the *Living Example Problems*, where one varies the parameters to explore the problem and to carry out a sensitivity analysis. For example, *what if someone suggested that you should double the catalyst particle diameter, what would you say?*
- 

<http://umich.edu/~scps/html/06chap/frames.htm>, while 12 Things You Can Do To Improve Your Creativity can be found at <http://www.umich.edu/~elements/5e/probsolv/strategy/creative.htm>. Osborn and deBono's brainstorming techniques, along with futuring, analogy, cross-fertilization, and TRIZ techniques TRIZ, can be found at <http://www.umich.edu/~scps/html/07chap/frames.htm> and [http://www.umich.edu/~elements/5e/toc/SCPS,3rdEdBook\(Ch07\).pdf](http://www.umich.edu/~elements/5e/toc/SCPS,3rdEdBook(Ch07).pdf).

One of the major goals at the undergraduate level is to bring students to the point where they can solve complex reaction problems, such as multiple reactions with heat effects, and then ask "What if . . . ?" questions and look for optimum operating conditions and unsafe operating conditions. The solution to one problem exemplifies this goal: the Manufacture of Styrene (Chapter 12, Problem P12-26<sub>c</sub>). This problem is particularly interesting because two reactions are endothermic and one is exothermic.

- (1) Ethylbenzene → Styrene + Hydrogen: Endothermic
- (2) Ethylbenzene → Benzene + Ethylene: Endothermic
- (3) Ethylbenzene + Hydrogen → Toluene + Methane: Exothermic

The student could get further practice in critical and creative thinking skills by adding any of the following exercises (x), (y), and (z) to any of the end-of-chapter homework problems.

- (x) How could you make this problem easier? More difficult?
- (y) Critique your answer by writing a critical thinking question.
- (z) Describe two ways you could work this problem incorrectly.



To summarize, it is this author's experience that both critical and creative thinking skills can be enhanced by using Tables P-2, P-3, and P-4 to extend any of the homework problems at the end of each chapter.

## H. What's New in This Edition?

### H.1 Pedagogy

This book maintains all the strengths of the first edition of *Essentials of Chemical Reaction Engineering* by using algorithms that allow students to learn chemical reaction engineering through logic rather than memorization. At the same time, this edition provides new resources that allow students to go beyond solving equations in order to get an intuitive feel and understanding of how reactors behave under different situations. Taken together the text and the associated Web site represent a mini-paradigm shift in the learning of chemical reaction engineering. This shift is achieved using Inquiry-Based Learning<sup>10</sup> (IBL) and the interaction between the text and the Web site's Living Example Problems (LEPs), as discussed in Preface Section D.2. The advent of Wolfram on CRE is one of the things that facilitated this paradigm shift.

Creative thinking skills can be enhanced by exploring the example problems and asking "What if . . . ?" questions, by using one or more of the brainstorming exercises in Table P-4 to extend any of the homework problems, and by solving the open-ended problems. For example, in the case study on safety, students can use the LEP on the CRE Web site to carry out a postmortem analysis on the nitroaniline explosion in Example 13-2 to learn what would have happened if the cooling had failed for five minutes instead of ten minutes. To this end, a new feature in the text is an Analysis paragraph at the end of each example problem. Significant effort has been devoted to developing example and homework problems that foster critical and creative thinking.

In this edition there are more than 80 interactive simulations (LEPs) provided on the Web site. The Web site has been greatly expanded to address the Felder/Solomon Inventory of Different Learning Styles<sup>11</sup> through interactive Summary Notes, i>clicker questions and Interactive Computer Games (ICGs). For example, as discussed in Appendix I the Global Learner can get an overview of the chapter material from the Summary Notes; the Sequential Learner can use all the i>clicker questions and  hot buttons; and the active learner can interact with the ICGs and use the  hot buttons in the Summary Notes.

To develop critical thinking skills, instructors can assign one of the new homework problems on troubleshooting, as well as ask the students to expand homework problems by asking a related question that involves critical thinking using Tables P-2 and P-3.

The following areas have an increased emphasis on the Web site for this new edition thorough interactive example problems using Polymath, Wolfram, and MATLAB:

1. Safety: Three industrial explosions are discussed and modeled.
  - a. Ammonium Nitrate CSTR Explosion (Chapters 12 and 13)
  - b. Nitroaniline Batch Reactor Runaway (Chapter 13)
  - c. T2 Laboratories Batch Reactor Runaway (Chapter 13)
  - d. Resources from SChE and CCPS (Chapter 12)

---

<sup>10</sup> Yet to receive

<sup>11</sup> <http://www.ncsu.edu/felder-public/ILSdir/styles.htm>

2. AspenTech: An AspenTech tutorial for chemical reaction engineering and four example problems are provided on the CRE Web site. The example problems are
  - a. Production of Ethylene from Ethane
  - b. The Pyrolysis of Benzene
  - c. Adiabatic Liquid Phase Isomerization of Normal Butane
  - d. Adiabatic Production of Acetic Anhydride

**And most importantly we have to always remember that:**

*Hopefully, all intensive laws tend often to have exceptions. Very important concepts take orderly, responsible statements. Virtually all laws intrinsically are natural thoughts. General observations become laws under experimentation.*

## I. How Do I Say Thank You?

There are so many colleagues and students who contributed to this book that it would require another chapter to thank them all in an appropriate manner. I again acknowledge all my friends, students, and colleagues for their contributions to the second edition of *Essentials of Chemical Reaction Engineering*. I would like to give special recognition as follows.

First of all, I am indebted to Ame and Catherine Vennema, whose gift of an endowed chair greatly facilitated the completion of this project. My colleague Dr. Nihat Gürmen coauthored the original Web site during the writing of the fourth edition of *Elements of Chemical Reaction Engineering*. He has been a wonderful colleague to work with. I also would like to thank University of Michigan undergraduate students Arthur Shih, Maria Quigley, Brendan Kirchner, and Ben Griessmann who worked on earlier versions of the Web site.

Michael B. Cutlip, coauthor of *Polymath*, not only gave suggestions and a critical reading of the first edition, but also, most importantly, provided continuous support and encouragement throughout the course of this project. Professor Chau-Chyun Chen provided two AspenTech examples. Ed Fontes at COMSOL Mutiphysics not only provided encouragement, but also provided a COMSOL Web site containing a tutorial with CRE examples. Julie Nahil, full-service production manager at Prentice Hall for all of my book projects, has been fantastic throughout. She provided encouragement, attention to detail, and a great sense of humor, which were greatly appreciated. Indian Institute of Technology (IIT)-Guwahati chemical engineering graduate Mayur Tikmani was amazing in helping to get this text to the compositor in time. He provided all of the Wolfram coding for the LEP examples; when necessary, checked and corrected all the *Polymath*, Wolfram and MATLAB tutorials on the CRE Web site; and also helped proofread all the chapters. Summer interns, Kaushik Nagaraj (IIT-Bombay, India) and Jakub Włodarczyk (Warsaw University of Technology, Poland) helped proofreading both the galley proofs and page proofs. Kaushik updated parts of the solution manual and the MATLAB coding in section 3.5 while Jakub checked all of the i>clicker questions and solutions. Kyungjun Kim and Wen He, computer science engineering (CSE) students at the University of Michigan did an excellent job in redesigning a major part of the Web site and inserted links and material throughout the Web site. University of Michigan students, Julia Faeth and Eric O'Neill each contributed an original problem to

Chapter 5. Professor Heather Mays at the University of Michigan gave comments on the draft chapters and on the i>clicker questions as she taught the course during winter term 2017. Thanks Mayur, Kaushik, Jakub, Jun, Wen, Julia, Eric, and Heather.

I very much appreciated the patience of my Ph.D. students during the period in which this edition was written. Thanks to Mark Sheng Zheng, Cláudio Vilas Bôas Fávero, and Luqman Hakim Bin Ahmad Mahir.

I would like to thank the following people for various different reasons: David Bogle, Lee Brown, Hank Browning, John Chen, Stu Churchill, Jim Duderstadt, Tom Edgar, John Falconer, Rich Felder, Asterios Gavriilidis, Joe Goddard, Robert Hesketh, Mark Hoefner, Jay Jorgenson, Lloyd Kemp, Costas Kravaris, Steve LeBlanc, Charlie Little, Kasper Lund, the Magnuson family, Joe Martin, Susan Montgomery, our parents, Guiseppe Parravano, Max Peters, Sid Sapakie, Phil Savage, Jerry Schultz, Johannes Schwank, Mordechai Shacham, Michael Stamatakis, Klaus Timmerhaus, Jim Wilkes, June Wispelwey, Max, Joe (aka “Jofo”), Sophia, Nicolas, the Emeritus Faculty Friday Lunch Group, and the Starbucks staff at Plymouth Road Mall, where most of my final editing of this book was accomplished.

Laura Bracken is very much a part of this book. I appreciate her excellent deciphering of equations and scribbles, her organization, her discovery of mistakes and inconsistencies, and her attention to detail in working with the galleys and proofs. Through all this was her ever-present wonderful disposition. Thanks, Radar!!

Finally, to my wife Janet, love and thanks. Not only did she type the first edition of this book—can you believe on a Royal Select typewriter!—she also was a sounding board for so many things in this edition. She was always willing to help with the wording and sentence structure. For example, I often asked her, “Is this the correct phrase or word to use here?” or “Should I mention Jofostan here?” Jan also helped me learn that creativity also involves knowing what to leave out. Without her enormous help and support the project would never have been possible.

HSF

Ann Arbor, Michigan  
August 2017



For updates and new and exciting applications, go to the Web site:

<http://www.umich.edu/~elements/5e/index.html>

For typographical errors, click on Updates & FAQ on the Home page to find

<http://www.umich.edu/~elements/5e/updates/index.html>

# About the Author



**H. Scott Fogler** is the Ame and Catherine Vennema professor of chemical engineering and the Arthur F. Thurnau professor at the University of Michigan in Ann Arbor, and was the 2009 National President of the American Institute of Chemical Engineers, a 50,000-member organization. He received his B.S. from the University of Illinois and his M.S. and Ph.D. from the University of Colorado. He is also the author of the *Essentials of Chemical Reaction Engineering, Fifth Edition*, and co-author, with Steven LeBlanc and Benjamin Rizzo, of *Strategies for Creative Problem Solving, Third Edition*.

Professor Fogler's research interests include flow and reaction in porous media, wax and asphaltene deposition, asphaltene flocculation kinetics, gelation kinetics, colloidal phenomena, and catalyzed dissolution. He has been research advisor to more than forty-five Ph.D. students and has more than two hundred forty refereed publications in these areas. Fogler has chaired ASEE's Chemical Engineering Division, served as director of the American Institute of Chemical Engineers, and earned the Warren K. Lewis Award from AIChE for contributions to chemical engineering education. He also received the Chemical Manufacturers Association's National Catalyst Award and the 2010 Malcom E. Pruitt Award from the Council for Chemical Research (CCR). He is the recipient of 11 named lectureships and is associate editor of *Energy & Fuels*. On April 15, 2016, Scott received a *doctor honoris causa* degree from the Universitat Rovira i Virgili, Tarragona, Spain.



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# *Mole Balances* 1

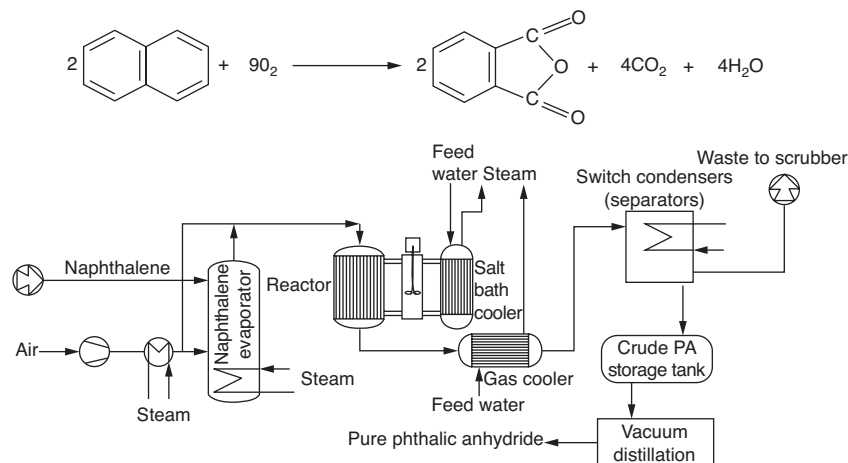
The first step to knowledge  
is to know that we are ignorant.

—Socrates (470–399 B.C.)

## **The Wide Wild World of Chemical Reaction Engineering**

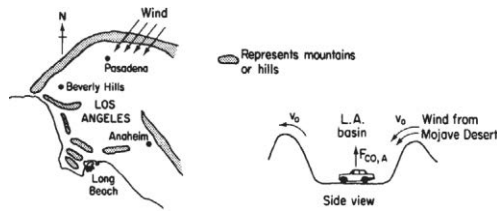
How is a chemical  
engineer different  
from other  
engineers?

Chemical kinetics is the study of chemical reaction rates and reaction mechanisms. The study of chemical reaction engineering (CRE) combines the study of chemical kinetics with the reactors in which the reactions occur. Chemical kinetics and reactor design are at the heart of producing almost all industrial chemicals, such as the manufacture of phthalic anhydride shown in Figure 1-1. It is primarily a knowledge of chemical kinetics and reactor design that distinguishes the chemical engineer from other engineers. The selection of a reaction system that operates in the safest and most efficient manner can be the key to the economic success or failure of a chemical plant. For example, if a reaction system produces a large amount of undesirable product, subsequent purification and separation of the desired product could make the entire process economically unfeasible.

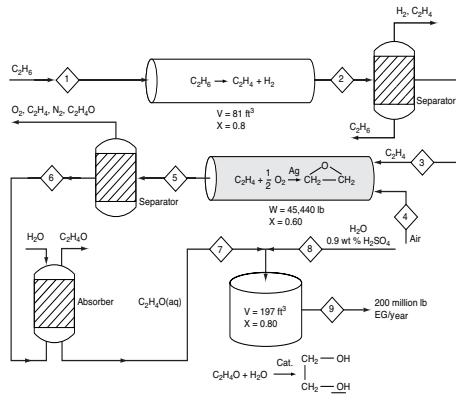


**Figure 1-1** Manufacture of phthalic anhydride.

The chemical reaction engineering (**CRE**) principles learned here can also be applied in many areas, such as waste treatment, microelectronics, nanoparticles, and living systems, in addition to the more traditional areas of the manufacture of chemicals and pharmaceuticals. Some of the examples that illustrate the wide application of CRE principles in this book are shown in Figure 1-2. These examples include modeling smog in the Los Angeles (L.A.) basin (Chapter 1), the digestive system of a hippopotamus (Chapter 2 on the CRE Web site, [www.umich.edu/~elements/5e/index.html](http://www.umich.edu/~elements/5e/index.html)), and molecular CRE (Chapter 3). Also shown are the manufacture of ethylene glycol (antifreeze), where three of the most common types of industrial reactors are used (Chapters 5 and 6), and the use of wetlands to degrade toxic chemicals (Chapter 7 on the CRE Web site). Other examples shown are the solid-liquid kinetics of acid-rock interactions to improve oil recovery (Chapter 7); pharmacokinetics of cobra bites (Chapter 8 Web Module); free-radical scavengers used in the design of motor oils (Chapter 9); enzyme kinetics (Chapter 9) and drug delivery pharmacokinetics (Chapter 9 on the CRE Web site); heat effects, runaway reactions, and plant safety (Chapters 11 through 13); and increasing the octane number of gasoline and the manufacture of computer chips (Chapter 10).



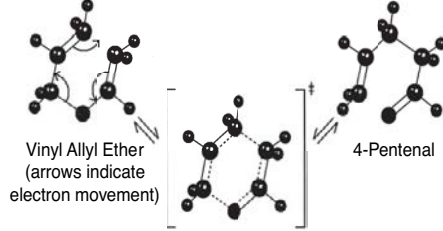
Smog (Ch. 1 on CRE Web site)



Chemical Plant for Ethylene Glycol (Ch. 5)

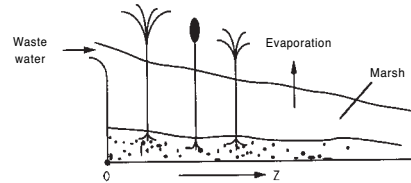


Hippo Digestion (Ch. 2 on CRE Web site)



Transition State (dashed lines show transition state electron delocalization)

Molecular CRE (Ch. 3 on CRE Web site)



Wetlands Remediation of Pollutants (Ch. 7 on CRE Web site)

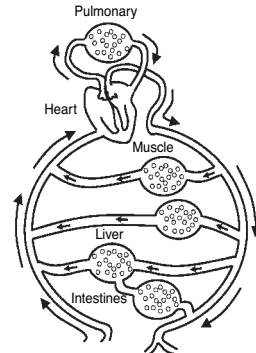


Pharmacokinetics of Cobra Bites  
Multiple Reactions in a Batch (Body) Reactor

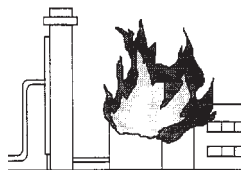
Cobra Bites (Ch. 8 on the CRE Web site)



Effective Lubricant Design Scavenging Free Radicals  
Lubricant Design (Ch. 9)

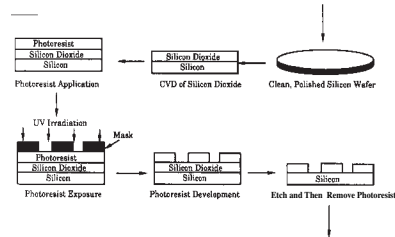


Pharmacokinetics (Ch. 9 on CRE Web site)



Nitroaniline Plant Explosion Exothermic Reactions That Run Away  
Plant Safety (Ch.11 to Ch.13)

(<http://www.umich.edu/~safeche/index.html>)



Microelectronic Fabrication Steps (Ch. 10)

Figure 1-2 The wide world of CRE applications.

**Overview.** This chapter develops the first building block of chemical reaction engineering, *mole balances*, which will be used continually throughout the text. After completing this chapter, the reader will be able to:

- Describe and define the rate of reaction
- Derive the general mole balance equation
- Apply the general mole balance equation to the four most common types of industrial reactors

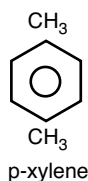
Before entering into discussions of the conditions that affect chemical reaction rate mechanisms and reactor design, it is necessary to account for the various chemical species entering and leaving a reaction system. This accounting process is achieved through overall mole balances on individual species in the reacting system. In this chapter, we develop a general mole balance that can be applied to any species (usually a chemical compound) entering, leaving, and/or remaining within the reaction system volume. After defining the rate of reaction,  $-r_A$ , we show how the general balance equation may be used to develop a preliminary form of the design equations of the most common industrial reactors (<http://encyclopedia.che.engin.umich.edu/Pages/Reactors/menu.html>).

- Batch Reactor (BR)
- Continuous-Stirred Tank Reactor (CSTR)
- Plug-Flow Reactor (PFR)
- Packed-Bed Reactor (PBR)

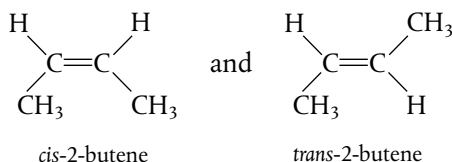
In developing these equations, the assumptions pertaining to the modeling of each type of reactor are delineated. Finally, a brief summary and series of short review questions are given at the end of the chapter.

## 1.1 The Rate of Reaction, $-r_A$

The rate of reaction tells us how fast a number of moles of one chemical species are being consumed to form another chemical species. The term *chemical species* refers to any chemical component or element with a given *identity*. The identity of a chemical species is determined by the *kind*, *number*, and *configuration* of that species' atoms. For example, the species para-xylene is made up of a fixed number of specific atoms in a definite molecular arrangement or configuration. The structure shown illustrates the kind, number, and configuration of atoms on a molecular level. Even though two chemical compounds have exactly the same kind and number of atoms of each element, they could still be different species because of different configurations. For example, 2-butene has four carbon atoms and eight hydrogen atoms; however, the atoms in this compound can form two different arrangements.



Identify – Kind – Number – Configuration
---



As a consequence of the different configurations, these two isomers display different chemical and physical properties. Therefore, we consider them as two different species, even though each has the same number of atoms of each element.

When has a chemical reaction taken place?

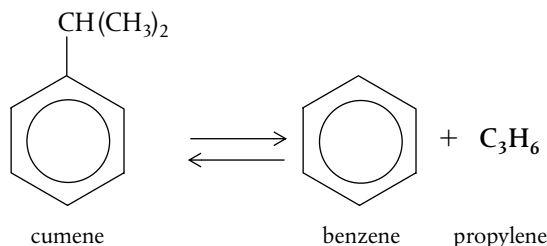
Definition of Rate of Reaction

We say that a *chemical reaction* has taken place when a detectable number of molecules of one or more species have lost their identity and assumed a new form by a change in the kind or number of atoms in the compound and/or by a change in structure or configuration of these atoms. In this classical approach to chemical change, it is assumed that the total mass is neither created nor destroyed when a chemical reaction occurs. The mass referred to is the total collective mass of all the different species in the system. However, when considering the individual species involved in a particular reaction, we do speak of the rate of disappearance of mass of a particular species. *The rate of disappearance of a species, say species A, is the number of A molecules that lose their chemical identity per unit time per unit volume through the breaking and subsequent re-forming of chemical bonds during the course of the reaction.* In order for a particular species to “appear” in the system, some prescribed fraction of another species must lose its chemical identity.

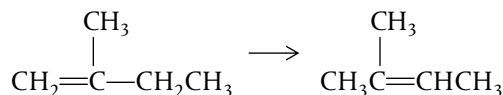
There are three basic ways a species may lose its chemical identity: decomposition, combination, and isomerization. In *decomposition*, the molecule loses its identity by being broken down into smaller molecules, atoms, or atom fragments. For example, if benzene and propylene are formed from a cumene molecule,

A species can lose its identity by

- Decomposition
- Combination
- Isomerization



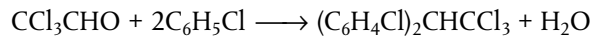
the cumene molecule has lost its identity (i.e., disappeared) by breaking its bonds to form these molecules. A second way that a molecule may lose its chemical identity is through *combination* with another molecule or atom. In the above reaction, the propylene molecule would lose its chemical identity if the reaction were carried out in the reverse direction, so that it combined with benzene to form cumene. The third way a species may lose its chemical identity is through *isomerization*, such as the reaction



Here, although the molecule neither adds other molecules to itself nor breaks into smaller molecules, it still loses its identity through a change in configuration.

To summarize this point, we say that a given number of molecules (i.e., moles) of a particular chemical species have reacted or disappeared when the molecules have lost their chemical identity.

The rate at which a given chemical reaction proceeds can be expressed in several ways. To illustrate, consider the reaction of chloral with chlorobenzene to produce the banned insecticide DDT (dichlorodiphenyl-trichloroethane) in the presence of fuming sulfuric acid.



Letting the symbol A represent chloral, B be chlorobenzene, C be DDT, and D be H<sub>2</sub>O, we obtain



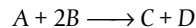
The numerical value of the rate of disappearance of reactant A,  $-r_A$ , is a positive number.

What is  $-r_A$ ?

The rate of reaction,  $-r_A$ , is the number of moles of A (e.g., chloral) reacting (disappearing) per unit time per unit volume ( $\text{mol}/\text{dm}^3\cdot\text{s}$ ).

### Example 1-1 Rates of Disappearance and Formation

Chloral is being consumed at a rate of 10 moles per second per  $\text{m}^3$  when reacting with chlorobenzene to form DDT and water in the reaction described above. In symbol form, the reaction is written as

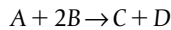


Write the rates of disappearance and formation (i.e., generation) for each species in this reaction.

*Solution*

- (a) *Chloral*[A]: The rate of reaction of chloral [A] ( $-r_A$ ) is given as  $10 \text{ mol}/\text{m}^3\cdot\text{s}$   
Rate of disappearance of A =  $-r_A = 10 \text{ mol}/\text{m}^3\cdot\text{s}$   
Rate of formation of A =  $r_A = -10 \text{ mol}/\text{m}^3\cdot\text{s}$
- (b) *Chlorobenzene*[B]: For every mole of chloral that disappears, two moles of chlorobenzene [B] also disappear.  
Rate of disappearance of B =  $-r_B = 20 \text{ mol}/\text{m}^3\cdot\text{s}$   
Rate of formation of B =  $r_B = -20 \text{ mol}/\text{m}^3\cdot\text{s}$
- (c) *DDT*[C]: For every mole of chloral that disappears, one mole of DDT[C] appears.  
Rate of formation of C =  $r_C = 10 \text{ mol}/\text{m}^3\cdot\text{s}$   
Rate of disappearance of C =  $-r_C = -10 \text{ mol}/\text{m}^3\cdot\text{s}$
- (d) *Water*[D]: Same relationship to chloral as the relationship to DDT  
Rate of formation of D =  $r_D = 10 \text{ mol}/\text{m}^3\cdot\text{s}$   
Rate of disappearance of D =  $-r_D = -10 \text{ mol}/\text{m}^3\cdot\text{s}$

$$\begin{aligned} -r_A &= 10 \text{ mol A}/\text{m}^3\cdot\text{s} \\ r_A &= -10 \text{ mol A}/\text{m}^3\cdot\text{s} \\ \text{Equation (3-1) page 73} \\ \text{Then} \\ \frac{r_A}{-1} &= \frac{r_B}{-2} = \frac{r_C}{1} = \frac{r_D}{1} \\ r_B &= 2(r_A) = -20 \text{ mol B}/\text{m}^3\cdot\text{s} \\ -r_B &= 20 \text{ mol B}/\text{m}^3\cdot\text{s} \\ r_C &= -r_A = 10 \text{ mol C}/\text{m}^3\cdot\text{s} \\ r_D &= -r_A = 10 \text{ mol D}/\text{m}^3\cdot\text{s} \end{aligned}$$



The convention

$-r_A = 10 \text{ mol A/m}^3\cdot\text{s}$
$r_A = -10 \text{ mol A/m}^3\cdot\text{s}$
$-r_B = 20 \text{ mol B/m}^3\cdot\text{s}$
$r_B = -20 \text{ mol B/m}^3\cdot\text{s}$
$r_C = 10 \text{ mol C/m}^3\cdot\text{s}$

**Analysis:** The purpose of this example is to better understand the convention for the rate of reaction. The symbol  $r_j$  is the rate of formation (generation) of species  $j$ . If species  $j$  is a reactant, the numerical value of  $r_j$  will be a negative number. If species  $j$  is a product, then  $r_j$  will be a positive number. The rate of reaction,  $-r_A$ , is the rate of disappearance of reactant A and must be a positive number. A mnemonic relationship to help remember how to obtain relative rates of reaction of A to B, etc., is given by Equation (3-1) on page 73.

In Chapter 3, we will delineate the prescribed relationship between the rate of formation of one species,  $r_j$  (e.g., DDT [C]), and the rate of disappearance of another species,  $-r_i$  (e.g., chlorobenzene [B]), in a chemical reaction.

Heterogeneous reactions involve more than one phase. In heterogeneous reaction systems, the rate of reaction is usually expressed in measures other than volume, such as reaction surface area or catalyst weight. For a gas-solid catalytic reaction, the gas molecules must interact with the solid catalyst surface for the reaction to take place, as described in Chapter 10.

What is  $-r'_A$ ? The dimensions of this heterogeneous reaction rate,  $-r'_A$  (prime), are the number of moles of A reacting per unit time per unit mass of catalyst (mol/s-g catalyst).

Definition of  $r_j$  Most of the introductory discussions on chemical reaction engineering in this book focus on homogeneous systems, in which case we simply say that  $r_j$  is the rate of formation of species  $j$  per unit volume. It is the number of moles of species  $j$  generated per unit volume per unit time.

We can say four things about the reaction rate  $r_j$ . The reaction rate law for  $r_j$  is

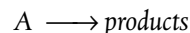
The rate law does not depend on the type of reactor used!!

- **The rate of formation of species  $j$  (mole/time/volume)**
- **An algebraic equation**
- **Independent of the type of reactor (e.g., batch or continuous flow) in which the reaction is carried out**
- **Solely a function of the properties of the reacting materials and reaction conditions (e.g., species concentration, temperature, pressure, or type of catalyst, if any) at a point in the system**

What is  $-r_A$  a function of?

However, because the properties and reaction conditions of the reacting materials may vary with position in a chemical reactor,  $r_j$  can in turn be a function of position and can vary from point to point in the system.

The chemical reaction rate law is essentially an algebraic equation involving concentration, not a differential equation.<sup>1</sup> For example, the algebraic form of the rate law for  $-r_A$  for the reaction



may be a linear function of concentration,

$$-r_A = kC_A \quad (1-1)$$

or it may be some other algebraic function of concentration, such as Equation 3-6 shown in Chapter 3

<sup>1</sup> For further elaboration on this point, see *Chem. Eng. Sci.*, 25, 337 (1970); B. L. Crynes and H. S. Fogler, eds., *AIChE Modular Instruction Series E: Kinetics*, 1, 1 (New York: AIChE, 1981); and R. L. Kabel, "Rates," *Chem. Eng. Commun.*, 9, 15 (1981).



$$-r_A = kC_A^2 \quad (1-2)$$

or

The rate law is an algebraic equation.

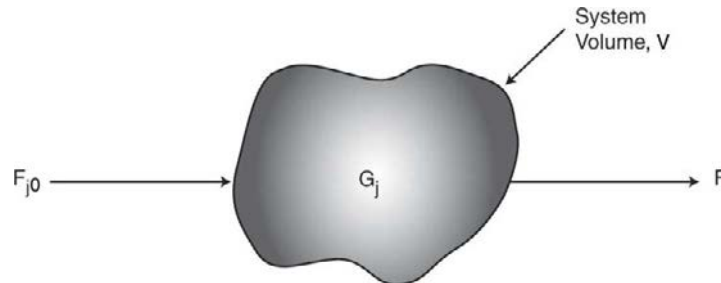
$$-r_A = \frac{k_1 C_A}{1 + k_2 C_A}$$

The convention

For a given reaction, the particular concentration dependence that the rate law follows (i.e.,  $-r_A = kC_A$  or  $-r_A = kC_A^2$  or ...) must be determined from *experimental observation*. Equation (1-2) states that the rate of disappearance of A is equal to a rate constant  $k$  (which is a function of temperature) times the square of the concentration of A. As noted earlier, by convention,  $r_A$  is the rate of formation of A; consequently,  $-r_A$  is the rate of disappearance of A. Throughout this book, the phrase *rate of generation* means exactly the same as the phrase *rate of formation*, and these phrases are used interchangeably.

## 1.2 The General Mole Balance Equation

To perform a mole balance on any system, the system boundaries must first be specified. The volume enclosed by these boundaries is referred to as the *system volume*. We shall perform a mole balance on species  $j$  in a system volume, where species  $j$  represents the particular chemical species of interest, such as water or NaOH (Figure 1-3).



**Figure 1-3** Mole balance on species  $j$  in a system volume,  $V$ .

A mole balance on species  $j$  at any instant in time,  $t$ , yields the following equation:

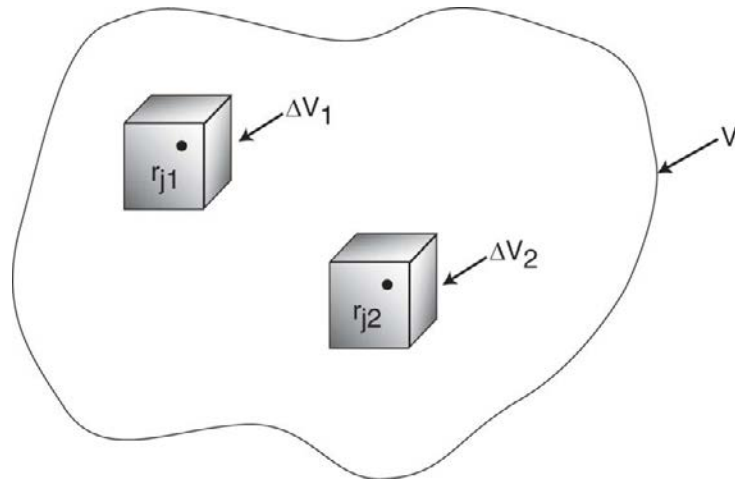
$$\begin{array}{l}
 \left[ \begin{array}{c} \text{Rate of flow} \\ \text{of } j \text{ into} \\ \text{the system} \\ \text{(moles/time)} \end{array} \right] - \left[ \begin{array}{c} \text{Rate of flow} \\ \text{of } j \text{ out of} \\ \text{the system} \\ \text{(moles/time)} \end{array} \right] + \left[ \begin{array}{c} \text{Rate of generation} \\ \text{of } j \text{ by chemical} \\ \text{reaction within} \\ \text{the system} \\ \text{(moles/time)} \end{array} \right] = \left[ \begin{array}{c} \text{Rate of} \\ \text{accumulation} \\ \text{of } j \text{ within} \\ \text{the system} \\ \text{(moles/time)} \end{array} \right] \\
 \text{Mole balance} \quad \mathbf{In} \quad - \quad \mathbf{Out} \quad + \quad \mathbf{Generation} \quad = \quad \mathbf{Accumulation} \\
 F_{j0} \quad - \quad F_j \quad + \quad G_j \quad = \quad \frac{dN_j}{dt} \quad (1-3)
 \end{array}$$

In this equation,  $N_j$  represents the number of moles of species  $j$  in the system at time  $t$ . If all the system variables (e.g., temperature, catalytic activity, and concentration of the chemical species) are spatially uniform throughout the system volume, the rate of generation of species  $j$ ,  $G_j$ , is just the product of the reaction volume,  $V$ , and the rate of formation of species  $j$ ,  $r_j$ .

$$G_j = r_j \cdot V$$

$$\frac{\text{moles}}{\text{time}} = \frac{\text{moles}}{\text{time} \cdot \text{volume}} \cdot \text{volume}$$

Now suppose that the rate of formation of species  $j$  for the reaction varies with position in the system volume. That is, it has a value  $r_{j1}$  at location 1, which is surrounded by a small volume,  $\Delta V_1$ , within which the rate is uniform; similarly, the reaction rate has a value  $r_{j2}$  at location 2 and an associated volume,  $\Delta V_2$ , and so on (Figure 1-4).



**Figure 1-4** Dividing up the system volume,  $V$ .

The rate of generation,  $\Delta G_{j1}$ , in terms of  $r_{j1}$  and subvolume  $\Delta V_1$ , is

$$\Delta G_{j1} = r_{j1} \Delta V_1$$

Similar expressions can be written for  $\Delta G_{j2}$  and the other system subvolumes,  $\Delta V_i$ . The total rate of generation within the system volume is the sum of all the rates of generation in each of the subvolumes. If the total system volume is divided into  $M$  subvolumes, the total rate of generation is

$$G_j = \sum_{i=1}^M \Delta G_{ji} = \sum_{i=1}^M r_{ji} \Delta V_i$$